

## **P1.T4. Valuation & Risk Models**

### **Chapter 1. Measures of Financial Risk**

#### **Bionic Turtle FRM Practice Questions**

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**Chapter 1. Measures of Financial Risk**

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# Chapter 1. Measures of Financial Risk

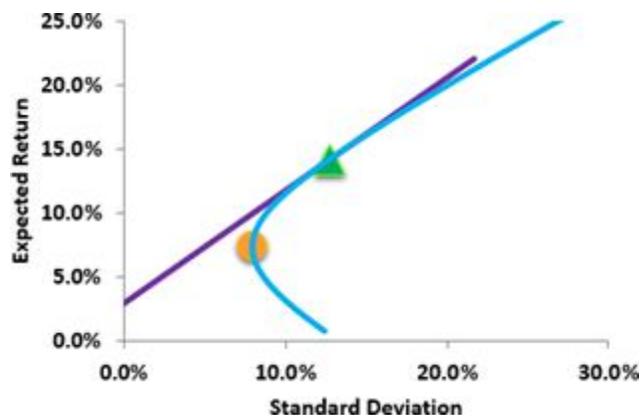
P1.T4.807. Classical value at risk (VaR)  
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## P1.T4.807. Classical value at risk (VaR)

**Learning objectives:** Describe the mean-variance framework and the efficient frontier. Explain the limitations of the mean-variance framework with respect to assumptions about return distributions.

807.1. Displayed below is a plot of the Capital Market Line (CML) according to the mean-variance framework. There are only two risky assets:

- Risky Asset A has an expected return and volatility of 8.0%
- Risky Asset B has an expected return and volatility of 20.0%



Please note the graph also contains an Orange Circle and a Green Triangle. About this situation, each of the following is true **EXCEPT** which is false?

- If the risk-free rate is constant at 3.0%, then the slope of the CML is invariant to the correlation between A & B returns
- An investor can achieve an expected return greater than 20.0%, which is the expected return of Risky Asset B, if she is willing to borrow at the risk-free rate
- The Green Triangle represents the Market Portfolio: it is entirely allocated between Risky Assets A & B but without any allocation to the risk-free asset
- The Orange Circle represents the Minimum Variance portfolio: it generates a Sharpe ratio that is inferior to (less than) the Sharpe ratio of any position on the CML

807.2. Dowd<sup>1</sup> explains that daily financial data can be expressed in either loss(+)/profit(-) format, or profit(+)/loss(-) format. For example, in profit(+)/loss(-) format which is more natural to the actual math, an asset's expected gain is represented by a positive value while its loss is represented by a negative. However, in risk it is also convenient to use loss(+)/profit(-) format such that losses are expressed by positive values.

Assume our chosen format is loss(+)/profit(-), which is also just called "L/P." Our position's profits are normally distributed and given by the following two parameters:

- The drift,  $\mu$ , is equal to  $-\$15.0$  per annum, and
- The volatility,  $\sigma$  is equal to  $\$35.0$  per annum.

If the daily returns are i.i.d. with 250 trading days per year, which is **nearest** to the 20-day 95.0% confident absolute value at risk (aVaR)?

- a) -9.35
- b) 15.08
- c) 21.83
- d) 42.57

807.3. Rebecca has determined that her equity portfolio's 25-day 95.0% confident absolute value at risk (aVaR) is given by  $-\mu \cdot \Delta t + \sigma \cdot \alpha \cdot \sqrt{\Delta t} = -12,000 + 208,000 = \$196,000$ . She subsequently decides that she wants to translate this into a 10-day 99.0% confident aVaR. If the returns are i.i.d. and normally distributed, which of the following is **nearest** to the translated VaR?

- a) 133,300
- b) 150,000
- c) 181,530
- d) 195,400

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<sup>1</sup> Kevin Dowd, Measuring Market Risk, 2nd Edition (West Sussex, England: John Wiley & Sons, 2005)

**Answers:**

**807.1. A. False: a change in correlation (Between Risky Asset A & B) will change the optimal Market Portfolio and therefore the slope of the CML**

In regard to (B), (C) and (D) each is TRUE.

**807.2. B. 15.08. As the 95.0% normal deviate is about 1.645, the 95.0% 20-day aVaR is given by  $-15 \cdot (20/250) + 35 \cdot \sqrt{20/250} \cdot 1.645 = \$15.08$ .**

**807.3. C. 181,530.**

The drift translates linearly:  $12,000 \cdot 10/25 = 4,800$ . The volatility translation includes two components:

- The time scales per the square root rule,  $\sqrt{10/25}$ , and further
- The confidence changes the deviate from  $\sim 1.645$  to  $\sim 2.33$ , proportionally per  $2.33/1.645$

Consequently, the volatility shock translates to  $208,000 \cdot \sqrt{10/25} \cdot 2.33/1.645 = \$186,330$ . Therefore the new 10-day 99.0% confident aVaR is given by  $-4,800 + 186,330 = 181,530$ .

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